

## NAG Library Function Document

### nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc)

#### 1 Purpose

nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc) may be used to supply optional arguments to nag\_glopt\_bnd\_mcs\_solve (e05jbc) from an external file. The initialization function nag\_glopt\_bnd\_mcs\_init (e05jac) **must** have been called before calling nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc).

#### 2 Specification

```
#include <nag.h>
#include <nage05.h>

void nag_glopt_bnd_mcs_optset_file (Nag_FileID fileid, Nag_E05State *state,
    NagError *fail)
```

#### 3 Description

nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc) may be used to supply values for optional arguments to nag\_glopt\_bnd\_mcs\_solve (e05jbc). nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc) reads an external file which has been opened by a call to nag\_open\_file (x04acc). Each line of the file defines a single optional argument. It is only necessary to supply values for those arguments whose values are to be different from their default values.

Each optional argument is defined by a single character string, consisting of one or more items. The items associated with a given optional argument must be separated by spaces, or equals signs [=]. Alphabetic characters may be upper or lower case. The string

```
Static Limit = 100
```

is an example of a string used to set an optional argument. For each optional argument the string contains one or more of the following items:

- a mandatory keyword;
- a phrase that qualifies the keyword;
- a number that specifies an integer or real value. Such numbers may be up to 16 contiguous characters.

Blank strings and comments are ignored. A comment begins with an asterisk (\*) and all subsequent characters in the string are regarded as part of the comment.

The implied data type (character, integer or real) of each value to set **must** match that expected by the corresponding optional argument.

The file containing the optional arguments must start with `Begin` and must finish with `End`. An example of a valid options file is:

```
Begin * Example options file
    Static Limit = 500
End
```

Optional argument settings are preserved following a call to nag\_glopt\_bnd\_mcs\_solve (e05jbc) and so the keyword **Defaults** is provided to allow you to reset all the optional arguments to their default values before a subsequent call to nag\_glopt\_bnd\_mcs\_solve (e05jbc).

A complete list of optional arguments, their symbolic names and default values is given in Section 12 in nag\_glopt\_bnd\_mcs\_solve (e05jbc).

## 4 References

None.

## 5 Arguments

- 1: **fileid** – Nag\_FileID *Input*  
*On entry:* the ID of the option file to be read, as returned by a call to nag\_open\_file (x04acc).
- 2: **state** – Nag\_E05State \* *Communication Structure*  
**state** contains information required by other functions in this suite. You must not modify it directly in any way.
- 3: **fail** – NagError \* *Input/Output*  
 The NAG error argument (see Section 3.6 in the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

### NE\_BAD\_PARAM

On entry, argument *<value>* had an illegal value.

### NE\_FILE\_NOT\_READ

At least one optional argument from the options file could not be recognized. *All optional arguments that were set from the file before this error was encountered will remain set on exit.*

BEGIN found, but end-of-file found before END. *All optional arguments that were set from the file before this error was encountered will remain set on exit.*

Could not read options file.

End-of-file found before BEGIN.

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

### NE\_NOT\_INIT

Initialization function nag\_glopt\_bnd\_mcs\_init (e05jac) has not been called.

### NE\_NOT\_PARSED

One of the numeric values to be set could not be parsed. Check that all such strings specify valid integer or real values.

### NE\_OUT\_OF\_RANGE

Attempt to assign an illegal value of **Local Searches** (*lscrch*): *lscrch* = "*<value>*".

Attempt to assign an illegal value of **Repeatability** (*repeat*): *repeat* = "*<value>*".

Attempt to assign a non-positive value of **Function Evaluations Limit** (*nf*): *nf* = *<value>*.

Attempt to assign a non-positive value of **Local Searches Limit** (*loclim*): *loclim* = *<value>*.

Attempt to assign a non-positive value of **Static Limit** (*stclim*): *stclim* = *<value>*.

Attempt to assign an out-of-bounds value of **Infinite Bound Size** (*infbnd*): *infbnd* =  $\langle value \rangle$ .

Attempt to assign too small a value of **Local Searches Tolerance** (*loctol*): *loctol* =  $\langle value \rangle$ .

Attempt to assign too small a value of **Target Objective Error** (*objerr*): *objerr* =  $\langle value \rangle$ .

Attempt to assign too small a value of **Target Objective Safeguard** (*objsg*): *objsg* =  $\langle value \rangle$ .

## 7 Accuracy

Not applicable.

## 8 Parallelism and Performance

Not applicable.

## 9 Further Comments

`nag_glopt_bnd_mcs_optset_string` (e05jdc), `nag_glopt_bnd_mcs_optset_char` (e05jec), `nag_glopt_bnd_mcs_optset_int` (e05jfc) or `nag_glopt_bnd_mcs_optset_real` (e05jgc) may also be used to supply optional arguments to `nag_glopt_bnd_mcs_solve` (e05jbc).

## 10 Example

This example finds the global minimum of the ‘peaks’ function in two dimensions

$$F(x, y) = 3(1 - x)^2 \exp(-x^2 - (y + 1)^2) - 10\left(\frac{x}{5} - x^3 - y^5\right) \exp(-x^2 - y^2) - \frac{1}{3} \exp(-(x + 1)^2 - y^2)$$

on the box  $[-3, 3] \times [-3, 3]$ .

The function  $F$  has several local minima and one global minimum in the given box. The global minimum is approximately located at  $(0.23, -1.63)$ , where the function value is approximately  $-6.55$ .

By specifying an initialization list via **list**, **numpts** and **initpt** we can start `nag_glopt_bnd_mcs_solve` (e05jbc) looking close to one of the local minima and check that it really does move away from that point to one of the global minima.

More precisely, we choose  $(-1, 0)$  as our initial point (see Section 10.3), and let the initialization list be

$$\begin{pmatrix} -3 & -1 & 3 \\ -3 & 0 & 3 \end{pmatrix}.$$

This example solves the optimization problem using some of the optional arguments described in Section 12 in `nag_glopt_bnd_mcs_solve` (e05jbc).

### 10.1 Program Text

```
/* nag_glopt_bnd_mcs_optset_file (e05jcc) Example Program.
 *
 * Copyright 2013 Numerical Algorithms Group.
 *
 * Mark 24, 2013.
 */
#include <string.h>
#include <stdio.h>
#include <math.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nage05.h>

#ifdef __cplusplus
extern "C" {
#endif
static void NAG_CALL objfun(Integer n, const double x[], double *f,
```

```

        Integer nstate, Nag_Comm *comm, Integer *inform);
static void NAG_CALL monit(Integer n, Integer ncall, const double xbest[],
        const Integer icount[], Integer sdlist,
        const double list[], const Integer numpts[],
        const Integer initpt[], Integer nbaskt,
        const double xbaskt[], const double boxl[],
        const double boxu[], Integer nstate, Nag_Comm *comm,
        Integer *inform);
static void NAG_CALL output_current_box(const double boxl[],
        const double boxu[]);
#ifdef __cplusplus
}
#endif

int main(void)
{
    /* Scalars */
    double          infbnd, obj;
    Integer          exit_status=0, i, ibdchk, n=2, nf, plot, sdlist, stclim;
    Nag_BoundType   boundenum;
    Nag_MCSInitMethod initmethodenum;
    /* Arrays */
    const char      *optionsfile = "e05jcce.opt";
    static double   ruser[2] = {-1.0, -1.0};
    char            bound[16], initmethod[18];
    double          *bl = 0, *bu = 0, *list = 0, *x = 0;
    char            lcsrch[3];
    Integer         *initpt = 0, *numpts = 0;
    Integer         iuser[1];
    /* Nag Types */
    Nag_E05State    state;
    NagError        fail;
    Nag_Comm        comm;
    Nag_FileID      fileid;

    INIT_FAIL(fail);

    printf("nag_glopt_bnd_mcs_optset_file (e05jcc) Example Program Results\n");

    /* For communication with user-supplied functions: */
    comm.iuser = iuser;
    comm.user = ruser;

    /* Skip heading in data file */
    scanf("%*[^\\n] ");
    /* Read sdlist from data file */
    scanf("%ld%*[^\\n] ", &sdlist);

    if (n <= 0 || sdlist <= 0)
        goto END;

    if (!(bl = NAG_ALLOC(n, double)) ||
        !(bu = NAG_ALLOC(n, double)) ||
        !(list = NAG_ALLOC(n*sdlist, double)) ||
        !(x = NAG_ALLOC(n, double)) ||
        !(initpt = NAG_ALLOC(n, Integer)) ||
        !(numpts = NAG_ALLOC(n, Integer)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Read in bound (and bl and bu if necessary) */
    scanf("%15s%*[^\\n] ", bound);

    /* nag_enum_name_to_value (x04nac).
     * Converts NAG enum member name to value
     */
    boundenum = (Nag_BoundType) nag_enum_name_to_value(bound);

```

```

if (boundenum == Nag_Bounds)
  /* Read in the whole of each bound */
  {
    for (i = 0; i < n; ++i)
      scanf("%lf", &bl[i]);
      scanf("%*[\n] ");

    for (i = 0; i < n; ++i)
      scanf("%lf", &bu[i]);
      scanf("%*[\n] ");
  }
else if (boundenum == Nag_BoundsEqual)
  /* Bounds are uniform: read in only the first entry of each */
  {
    scanf("%lf%*[\n] ", &bl[0]);
    scanf("%lf%*[\n] ", &bu[0]);
  }

/* Read in initmethod (and list, numpts and initpt if necessary) */
scanf("%17s%*[\n] ", initmethod);

/* nag_enum_name_to_value (x04nac).
 * Converts NAG enum member name to value
 */
initmethodenum = (Nag_MCSInitMethod) nag_enum_name_to_value(initmethod);

if (initmethodenum == Nag_UserSet)
  {
    for (i = 0; i < n*sdlist; ++i)
      scanf("%lf", &list[i]);
      scanf("%*[\n] ");

    for (i = 0; i < n; ++i)
      scanf("%ld", &numpts[i]);
      scanf("%*[\n] ");

    for (i = 0; i < n; ++i)
      scanf("%ld", &initpt[i]);
      scanf("%*[\n] ");
  }

/* Read in plot. Its value determines whether monit displays
 * information on the current search box
 */
scanf("%ld%*[\n] ", &plot);

/* Communicate plot through to monit */
iuser[0] = plot;

/* Call nag_glopt_bnd_mcs_init (e05jac) to initialize
 * nag_glopt_bnd_mcs_solve (e05jbc). */
/* Its first argument is a legacy argument and has no significance. */
nag_glopt_bnd_mcs_init(0, &state, &fail);

if (fail.code != NE_NOERROR)
  {
    printf("Initialization of nag_glopt_bnd_mcs_solve (e05jbc) failed.\n%s\n",
          fail.message);
    exit_status = 1;
    goto END;
  }

/* Use nag_glopt_bnd_mcs_optset_file (e05jcc) to read some options
 * from the end of the data file */

/* Call nag_open_file (x04acc) to set the stdin fileid. */
/* nag_open_file (x04acc).
 * Open unit number for reading, writing or appending, and
 * associate unit with named file
 */
nag_open_file(optionsfile, 0, &fileid, &fail);

```

```

if (fail.code != NE_NOERROR)
{
    printf("Fileid could not be obtained.\n");
    exit_status = 1;
    goto END;
}

/* nag_glopt_bnd_mcs_optset_file (e05jcc).
 * Supply optional parameter values for nag_glopt_bnd_mcs_solve (e05jbc)
 * from external file */
nag_glopt_bnd_mcs_optset_file(fileid, &state, &fail);

if (fail.code != NE_NOERROR)
{
    printf("nag_glopt_bnd_mcs_optset_file (e05jcc) failed.\n%s\n",
        fail.message);
    exit_status = 1;
    goto END;
}

/* Use nag_glopt_bnd_mcs_optget_int (e05jkc) to find the value of
 * the Integer-valued option 'Function Evaluations Limit' */
/* nag_glopt_bnd_mcs_optget_int (e05jkc).
 * Get the setting of an Integer-valued option of
 * nag_glopt_bnd_mcs_solve (e05jbc) */
nag_glopt_bnd_mcs_optget_int("Function Evaluations Limit", &nf, &state,
    &fail);

if (fail.code != NE_NOERROR)
{
    printf("nag_glopt_bnd_mcs_optget_int (e05jkc) failed.\n%s\n",
        fail.message);
    exit_status = 1;
    goto END;
}

printf("\nOption 'Function Evaluations Limit' has the value %ld.\n",
    nf);

/* Use nag_glopt_bnd_mcs_optset_int (e05jfc) to set the value of the
 * Integer-valued option 'Static Limit' */

stclim = 4*n;

/* nag_glopt_bnd_mcs_optset_int (e05jfc).
 * Set a single Integer-valued option of
 * nag_glopt_bnd_mcs_solve (e05jbc) */
nag_glopt_bnd_mcs_optset_int("Static Limit", stclim, &state, &fail);

if (fail.code != NE_NOERROR)
{
    printf("nag_glopt_bnd_mcs_optset_int (e05jfc) failed.\n%s\n",
        fail.message);
    exit_status = 1;
    goto END;
}

/* Use nag_glopt_bnd_mcs_option_check (e05jhc) to determine whether
 * the real-valued option 'Infinite Bound Size' has been set by us
 * (in which case 1 is returned) or whether it holds its default
 * value (in which case 0 is returned) */
/* nag_glopt_bnd_mcs_option_check (e05jhc).
 * Determine whether the user has set a single option of
 * nag_glopt_bnd_mcs_solve (e05jbc) */
ibdchk = nag_glopt_bnd_mcs_option_check("Infinite Bound Size", &state, &fail);

if (fail.code != NE_NOERROR)
{
    printf("nag_glopt_bnd_mcs_option_check (e05jhc) failed.\n%s\n",
        fail.message);
}

```

```

        exit_status = 1;
        goto END;
    }

    printf("Option 'Infinite Bound Size' ");
    printf((ibdchk == 1 ? "has been set by us" : "holds its default value"));
    printf(".\n");

    /* Use nag_glopt_bnd_mcs_optget_real (e05jlc) to find the value of
     * the real-valued option 'Infinite Bound Size' */
    /* nag_glopt_bnd_mcs_optget_real (e05jlc).
     * Get the setting of a real-valued option of
     * nag_glopt_bnd_mcs_solve (e05jbc) */
    nag_glopt_bnd_mcs_optget_real("Infinite Bound Size", &infbnd, &state, &fail);

    if (fail.code != NE_NOERROR)
    {
        printf("nag_glopt_bnd_mcs_optget_real (e05jlc) failed.\n%s\n",
            fail.message);
        exit_status = 1;
        goto END;
    }

    printf("Option 'Infinite Bound Size' has the value %14.5e\n", infbnd);

    /* Use nag_glopt_bnd_mcs_optset_real (e05jgc) to increase the value of
     * the real-valued option 'Infinite Bound Size' tenfold */

    infbnd = 10.0*infbnd;

    /* nag_glopt_bnd_mcs_optset_real (e05jgc).
     * Set the value of a real-valued option of
     * nag_glopt_bnd_mcs_solve (e05jbc) */
    nag_glopt_bnd_mcs_optset_real("Infinite Bound Size", infbnd, &state, &fail);

    if (fail.code != NE_NOERROR)
    {
        printf("nag_glopt_bnd_mcs_optset_real (e05jgc) failed.\n%s\n",
            fail.message);
        exit_status = 1;
        goto END;
    }

    /* Use nag_glopt_bnd_mcs_optset_string (e05jdc) to set the value of
     * the Integer-valued option 'Local Searches Limit' */
    /* nag_glopt_bnd_mcs_optset_string (e05jdc).
     * Set the value of an option of nag_glopt_bnd_mcs_solve (e05jbc)
     * from a string */
    nag_glopt_bnd_mcs_optset_string("Local Searches Limit = 40", &state, &fail);

    if (fail.code != NE_NOERROR)
    {
        printf("nag_glopt_bnd_mcs_optset_string (e05jdc) failed.\n%s\n",
            fail.message);
        exit_status = 1;
        goto END;
    }

    /* Use nag_glopt_bnd_mcs_optset_char (e05jec) to set the value of
     * the 'On'/'Off'-valued character option 'Local Searches' */
    strcpy(&lcsrch[0], "On");

    /* nag_glopt_bnd_mcs_optset_char (e05jec).
     * Set the value of an 'On'/'Off'-valued character option of
     * nag_glopt_bnd_mcs_solve (e05jbc) */
    nag_glopt_bnd_mcs_optset_char("Local Searches", lcsrch, &state, &fail);

    if (fail.code != NE_NOERROR)
    {
        printf("nag_glopt_bnd_mcs_optset_char (e05jec) failed.\n%s\n",
            fail.message);
    }

```

```

        exit_status = 1;
        goto END;
    }

/* Solve the problem. */
/* nag_glopt_bnd_mcs_solve (e05jbc).
 * Global optimization by multilevel coordinate search, simple bounds.
 */
nag_glopt_bnd_mcs_solve(n, objfun, boundenum, initmethodenum, bl, bu,
                        sdlist, list, numpts, initpt, monit, x, &obj,
                        &state, &comm, &fail);

if (fail.code != NE_NOERROR)
{
    printf("Error message from nag_glopt_bnd_mcs_solve (e05jbc).\n%s\n",
          fail.message);
    exit_status = 1;
    goto END;
}

printf("Final objective value = %11.5f\n", obj);
printf("Global optimum x = ");
for (i = 0; i < n; ++i)
    printf("%9.5f", x[i]);
printf("\n");

END:
NAG_FREE(bl);
NAG_FREE(bu);
NAG_FREE(list);
NAG_FREE(x);
NAG_FREE(initpt);
NAG_FREE(numpts);

return exit_status;
}

static void NAG_CALL objfun(Integer n, const double x[], double *f,
                           Integer nstate, Nag_Comm *comm, Integer *inform)
{
    /* Routine to evaluate objective function */

    if (comm->user[0] == -1.0)
    {
        printf("(User-supplied callback objfun, first invocation.)\n");
        comm->user[0] = 0.0;
    }

    /* This is a two-dimensional objective function.
     * As an example of using the inform mechanism,
     * terminate if any other problem size is supplied.
     */
    if (n!=2)
    {
        *inform = -1;
        return;
    }

    *inform = 0;

    if (*inform >= 0)
    /* Here we're prepared to evaluate objfun at the current x */
    {
        if (nstate == 1)
        /* This is the first call to objfun */
        {
            printf("\n(objfun was just called for the first time)\n");
        }

        *f = (
            3.0*pow((1.0-x[0]), 2)*exp(-pow(x[0], 2)-pow((x[1]+1), 2))

```



```

- (10.0*(x[0]/5.0-pow(x[0], 3)-pow(x[1], 5))*
  exp(-pow(x[0], 2)-pow(x[1], 2)))
- 1.0/3.0*exp(-pow((x[0]+1.0), 2)-pow(x[1], 2))
);
}
}

static void NAG_CALL monit(Integer n, Integer ncall, const double xbest[],
                          const Integer icount[], Integer sdlist,
                          const double list[], const Integer numpts[],
                          const Integer initpt[], Integer nbasket,
                          const double xbasket[], const double boxl[],
                          const double boxu[], Integer nstate, Nag_Comm *comm,
                          Integer *inform)
{
  /* Scalars */
  Integer i, j;
  Integer plot;

#define LIST(I, J) list[(I-1)*sdlist + (J-1)]
#define XBASKET(I, J) xbasket[(I-1)*nbasket + (J-1)]

  if (comm->user[1] == -1.0)
  {
    printf("(User-supplied callback monit, first invocation.)\n");
    comm->user[1] = 0.0;
  }

  *inform = 0;

  if (*inform >= 0)
  /* We are going to allow the iterations to continue */
  {
    /* Extract plot from the communication structure */
    plot = comm->iuser[0];

    if (nstate == 0 || nstate == 1)
    /* When nstate == 1, monit is called for the first time.
     * When nstate == 0, monit is called for the first AND last time.
     * Display a welcome message */
    {
      printf("\n*** Begin monitoring information ***\n\n");

      printf("Values controlling initial splitting of a box:\n");
      for (i = 1; i <= n; ++i)
      {
        printf("***\n");
        printf("In dimension %5ld\n", i);
        printf("Extent of initialization list in this dimension = "
              "%5ld\n", numpts[i - 1]);
        printf("Initialization points in this dimension:\n");
        printf("LIST(i, 1:numpts[i - 1]) =");
        for (j = 1; j <= numpts[i - 1]; ++j)
          printf("%9.5f", LIST(i, j));
        printf("\n");
        printf("Initial point in this dimension: LIST(i,%5ld)\n",
              initpt[i - 1]);
      }

      if (plot != 0 && n == 2)
        printf("<Begin displaying search boxes>\n\n");
    }

    if (plot != 0 && n == 2)
    {
      /* Display the coordinates of the edges of the current search box */
      output_current_box(boxl, boxu);
    }

    if (nstate <= 0)
    /* monit is called for the last time */

```

```

    {
        if (plot != 0 && n == 2)
            printf("<End displaying search boxes>\n\n");
        printf("Total sub-boxes = %5ld\n", icount[0]);
        printf("Total function evaluations = %5ld\n", ncall);
        printf("Total function evaluations used in local search = "
            "%5ld\n", icount[1]);
        printf("Total points used in local search = %5ld\n",
            icount[2]);
        printf("Total sweeps through levels = %5ld\n", icount[3]);
        printf("Total splits by init. list = %5ld\n", icount[4]);
        printf("Lowest level with nonsplit boxes = %5ld\n",
            icount[5]);
        printf("Number of candidate minima in the 'shopping basket'"
            " = %5ld\n", nbasket);
        printf("Shopping basket:\n");

        for (i = 1; i <= n; ++i)
            {
                printf("xbasket(%3ld,:) =", i);
                for (j = 1; j <= nbasket; ++j)
                    printf("%9.5f", XBASKT(i, j));
                printf("\n");
            }

        printf("Best point:\n");
        printf("xbest =");
        for (i = 0; i < n; ++i)
            printf("%9.5f", xbest[i]);
        printf("\n");

        printf("\n*** End monitoring information ***\n\n");
    }
}

static void NAG_CALL output_current_box(const double boxl[],
                                       const double boxu[])
{
    printf("%20.15f %20.15f\n", boxl[0], boxl[1]);
    printf("%20.15f %20.15f\n\n", boxl[0], boxu[1]);
    printf("%20.15f %20.15f\n", boxl[0], boxl[1]);
    printf("%20.15f %20.15f\n\n", boxu[0], boxl[1]);
    printf("%20.15f %20.15f\n", boxl[0], boxu[1]);
    printf("%20.15f %20.15f\n\n", boxu[0], boxu[1]);
    printf("%20.15f %20.15f\n", boxu[0], boxl[1]);
    printf("%20.15f %20.15f\n\n", boxu[0], boxu[1]);
}

```

## 10.2 Program Data

```

nag_glopt_bnd_mcs_optset_file (e05jcc) Example Program Data
 3                               : sdlist
Nag_Bounds                       : bound
-3.0  -3.0                       : Lower bounds bl
 3.0   3.0                       : Upper bounds bu
Nag_UserSet                       : initmethod
-3.0  -1.0   3.0  -3.0   0.0   3.0 : Matrix list
 3   3   3                       : numpts
 2   2   2                       : Initial-point pointer initpt
 0                               : plot

```

Begin example options file

```

* Comment lines like this begin with an asterisk
* Set the maximum number of function evaluations
Function Evaluations Limit = 100000
* Set the local search termination tolerance
Local Searches Tolerance = 1.0D-10
* Set the maximum number of times a given box may be split
Splits Limit = 20
End

```

### 10.3 Program Results

nag\_glopt\_bnd\_mcs\_optset\_file (e05jcc) Example Program Results

Option 'Function Evaluations Limit' has the value 100000.  
 Option 'Infinite Bound Size' holds its default value.  
 Option 'Infinite Bound Size' has the value 1.15792e+77  
 (User-supplied callback objfun, first invocation.)

(objfun was just called for the first time)  
 (User-supplied callback monit, first invocation.)

\*\*\* Begin monitoring information \*\*\*

Values controlling initial splitting of a box:

\*\*

In dimension 1  
 Extent of initialization list in this dimension = 3  
 Initialization points in this dimension:  
 LIST(i, 1:numpts[i - 1]) = -3.00000 -1.00000 3.00000  
 Initial point in this dimension: LIST(i, 2)  
 \*\*

In dimension 2  
 Extent of initialization list in this dimension = 3  
 Initialization points in this dimension:  
 LIST(i, 1:numpts[i - 1]) = -3.00000 0.00000 3.00000  
 Initial point in this dimension: LIST(i, 2)  
 Total sub-boxes = 180  
 Total function evaluations = 185  
 Total function evaluations used in local search = 102  
 Total points used in local search = 9  
 Total sweeps through levels = 9  
 Total splits by init. list = 5  
 Lowest level with nonsplit boxes = 6  
 Number of candidate minima in the 'shopping basket' = 2  
 Shopping basket:  
 xbask( 1,:) = 0.22828 -1.34740  
 xbask( 2,:) = -1.62553 0.20452  
 Best point:  
 xbest = 0.22828 -1.62553

\*\*\* End monitoring information \*\*\*

Final objective value = -6.55113  
 Global optimum x = 0.22828 -1.62553

**Example Program**  
The Peaks Function  $F$  and Search Boxes  
The global minimum is denoted by \*, while our start point is labelled with X

