e01 – Interpolation

# NAG Library Function Document

## nag 2d triang eval (e01skc)

#### 1 Purpose

nag\_2d\_triang\_eval (e01skc) evaluates at a given point the two-dimensional interpolant function computed by nag\_2d\_triang\_interp (e01sjc).

## 2 Specification

## 3 Description

nag\_2d\_triang\_eval (e01skc) takes as input the arguments defining the interpolant F(x,y) of a set of scattered data points  $(x_r, y_r, f_r)$ , for r = 1, 2, ..., m, as computed by nag\_2d\_shep\_interp (e01sgc), and evaluates the interpolant at the point (px, py).

If (px, py) is equal to  $(x_r, y_r)$  for some value of r, the returned value will be equal to  $f_r$ .

If (px, py) is not equal to  $(x_r, y_r)$  for any r, the derivatives in **grads** will be used to compute the interpolant. A triangle is sought which contains the point (px, py), and the vertices of the triangle along with the partial derivatives and  $f_r$  values at the vertices are used to compute the value F(px, py). If the point (px, py) lies outside the triangulation defined by the input arguments, the returned value is obtained by extrapolation. In this case, the interpolating function  $\mathbf{f}$  is extended linearly beyond the triangulation boundary. The method is described in more detail in Renka and Cline (1984) and the code is derived from Renka (1984).

nag\_2d\_triang\_eval (e01skc) must only be called after a call to nag\_2d\_shep\_interp (e01sgc).

#### 4 References

Renka R L (1984) Algorithm 624: triangulation and interpolation of arbitrarily distributed points in the plane ACM Trans. Math. Software 10 440-442

Renka R L and Cline A K (1984) A triangle-based  $C^1$  interpolation method *Rocky Mountain J. Math.* 14 223–237

## 5 Arguments

1:	m – Integer	Input
2:	$\mathbf{x}[\mathbf{m}]$ – const double	Input
3:	$\mathbf{y}[\mathbf{m}]$ – const double	Input
4:	f[m] – const double	Input
5:	$triang[7 \times m] - const Integer$	Input
6:	$grads[2 \times m]$ – const double	Input

On entry: m, x, y, f, triang and grads must be unchanged from the previous call of nag 2d triang interp (e01sjc).

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7:  $\mathbf{px}$  - double Input
8:  $\mathbf{py}$  - double Input

On entry: the point (px, py) at which the interpolant is to be evaluated.

9: **pf** – double \* Output

On exit: the value of the interpolant evaluated at the point (px, py).

10: **fail** – NagError \*

Input/Output

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

### 6 Error Indicators and Warnings

#### NE ALLOC FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

#### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

#### $NE\_INT$

On entry,  $\mathbf{m} = \langle value \rangle$ . Constraint:  $\mathbf{m} \geq 3$ .

#### NE INTERNAL ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

#### NE NO LICENCE

Your licence key may have expired or may not have been installed correctly. See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

#### NE TRIANG INVALID

On entry, **triang** does not contain a valid data point triangulation; **triang** may have been corrupted since the call to nag 2d triang interp (e01sjc).

#### NW VALUE EXTRAPOLATED

Warning – the evaluation point  $(\langle value \rangle, \langle value \rangle)$  lies outside the triangulation boundary. The returned value was computed by extrapolation.

#### 7 Accuracy

Computational errors should be negligible in most practical situations.

#### 8 Parallelism and Performance

nag\_2d\_triang\_eval (e01skc) is not threaded in any implementation.

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## 9 Further Comments

The time taken for a call of  $nag_2d_triang_eval$  (e01skc) is approximately proportional to the number of data points, m.

The results returned by this function are particularly suitable for applications such as graph plotting, producing a smooth surface from a number of scattered points.

## 10 Example

See Section 10 in nag\_2d\_shep\_interp (e01sgc).

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