NAG Library Function Document nag zunmrq (f08cxc)

1 Purpose

nag_zunmrq (f08cxc) multiplies a general complex m by n matrix C by the complex unitary matrix Q from an RQ factorization computed by nag zgerqf (f08cvc).

2 Specification

3 Description

 nag_zunmrq (f08cxc) is intended to be used following a call to nag_zgerqf (f08cvc), which performs an RQ factorization of a complex matrix A and represents the unitary matrix Q as a product of elementary reflectors.

This function may be used to form one of the matrix products

$$QC$$
, $Q^{H}C$, CQ , CQ^{H} ,

overwriting the result on C, which may be any complex rectangular m by n matrix.

A common application of this function is in solving underdetermined linear least squares problems, as described in the f08 Chapter Introduction, and illustrated in Section 10 in nag zgerqf (f08cvc).

4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia http://www.netlib.org/lapack/lug

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

5 Arguments

1: **order** – Nag_OrderType

Input

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.

Constraint: order = Nag_RowMajor or Nag_ColMajor.

2: **side** – Nag SideType

Input

On entry: indicates how Q or Q^{H} is to be applied to C.

side = Nag_LeftSide

Q or $Q^{\rm H}$ is applied to C from the left.

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```
\begin{aligned} \textbf{side} &= \text{Nag\_RightSide} \\ &\quad Q \text{ or } Q^{\text{H}} \text{ is applied to } C \text{ from the right.} \\ &\quad \textit{Constraint: } \textbf{side} &= \text{Nag\_LeftSide or Nag\_RightSide.} \end{aligned}
```

3: **trans** – Nag TransType

Input

On entry: indicates whether Q or Q^H is to be applied to C.

```
{f trans} = {f Nag\_NoTrans} Q is applied to C. {f trans} = {f Nag\_ConjTrans} Q^H is applied to C.
```

Constraint: trans = Nag_NoTrans or Nag_ConjTrans.

4: **m** – Integer

Input

On entry: m, the number of rows of the matrix C.

Constraint: $\mathbf{m} \geq 0$.

5: **n** – Integer

Input

On entry: n, the number of columns of the matrix C.

Constraint: $\mathbf{n} \geq 0$.

6: **k** – Integer

Input

On entry: k, the number of elementary reflectors whose product defines the matrix Q.

Constraints:

```
if side = Nag\_LeftSide, m \ge k \ge 0; if side = Nag\_RightSide, n \ge k \ge 0.
```

7: $\mathbf{a}[dim]$ - Complex

Input/Output

Note: the dimension, dim, of the array a must be at least

```
\max(1, \mathbf{pda} \times \mathbf{m}) when \mathbf{side} = \text{Nag\_LeftSide} and \mathbf{order} = \text{Nag\_ColMajor}; \max(1, \mathbf{k} \times \mathbf{pda}) when \mathbf{side} = \text{Nag\_LeftSide} and \mathbf{order} = \text{Nag\_RowMajor}; \max(1, \mathbf{pda} \times \mathbf{n}) when \mathbf{side} = \text{Nag\_RightSide} and \mathbf{order} = \text{Nag\_ColMajor}; \max(1, \mathbf{k} \times \mathbf{pda}) when \mathbf{side} = \text{Nag\_RightSide} and \mathbf{order} = \text{Nag\_RowMajor}.
```

The (i, j)th element of the matrix A is stored in

```
\mathbf{a}[(j-1) \times \mathbf{pda} + i - 1] when \mathbf{order} = \text{Nag\_ColMajor}; \mathbf{a}[(i-1) \times \mathbf{pda} + j - 1] when \mathbf{order} = \text{Nag\_RowMajor}.
```

On entry: the *i*th row of a must contain the vector which defines the elementary reflector H_i , for i = 1, 2, ..., k, as returned by nag_zgerqf (f08cvc).

On exit: is modified by nag_zunmrq (f08cxc) but restored on exit.

8: **pda** – Integer

Input

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **a**.

Constraints:

```
if order = Nag_ColMajor, pda \geq \max(1, \mathbf{k}); if order = Nag_RowMajor, if side = Nag_LeftSide, pda \geq \max(1, \mathbf{m}); if side = Nag_RightSide, pda \geq \max(1, \mathbf{n})..
```

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9: tau[dim] - const Complex

Input

Note: the dimension, dim, of the array tau must be at least max(1, k).

On entry: tau[i-1] must contain the scalar factor of the elementary reflector H_i , as returned by nag zgerqf (f08cvc).

10: $\mathbf{c}[dim]$ – Complex

Input/Output

Note: the dimension, dim, of the array **c** must be at least

```
\max(1, \mathbf{pdc} \times \mathbf{n}) when \mathbf{order} = \text{Nag\_ColMajor}; \max(1, \mathbf{m} \times \mathbf{pdc}) when \mathbf{order} = \text{Nag\_RowMajor}.
```

The (i, j)th element of the matrix C is stored in

```
\mathbf{c}[(j-1) \times \mathbf{pdc} + i - 1] when \mathbf{order} = \text{Nag\_ColMajor}; \mathbf{c}[(i-1) \times \mathbf{pdc} + j - 1] when \mathbf{order} = \text{Nag\_RowMajor}.
```

On entry: the m by n matrix C.

On exit: c is overwritten by QC or $Q^{H}C$ or CQ or CQ^{H} as specified by side and trans.

11: **pdc** – Integer

Input

On entry: the stride separating row or column elements (depending on the value of **order**) in the array \mathbf{c} .

Constraints:

```
if order = Nag_ColMajor, pdc \ge max(1, m); if order = Nag_RowMajor, pdc \ge max(1, n).
```

12: **fail** – NagError *

Input/Output

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

NE BAD PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE ENUM INT 3

```
On entry, \mathbf{side} = \langle value \rangle, \mathbf{m} = \langle value \rangle, \mathbf{n} = \langle value \rangle and \mathbf{k} = \langle value \rangle. Constraint: if \mathbf{side} = \text{Nag\_LeftSide}, \mathbf{m} \geq \mathbf{k} \geq 0; if \mathbf{side} = \text{Nag\_RightSide}, \mathbf{n} \geq \mathbf{k} \geq 0. On entry, \mathbf{side} = \langle value \rangle, \mathbf{pda} = \langle value \rangle, \mathbf{m} = \langle value \rangle and \mathbf{n} = \langle value \rangle. Constraint: if \mathbf{side} = \text{Nag\_LeftSide}, \mathbf{pda} \geq \max(1, \mathbf{m}); if \mathbf{side} = \text{Nag\_RightSide}, \mathbf{pda} \geq \max(1, \mathbf{n}).
```

NE INT

```
On entry, \mathbf{m} = \langle value \rangle.
Constraint: \mathbf{m} \geq 0.
On entry, \mathbf{n} = \langle value \rangle.
Constraint: \mathbf{n} \geq 0.
```

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```
On entry, \mathbf{pda} = \langle value \rangle.
Constraint: \mathbf{pda} > 0.
On entry, \mathbf{pdc} = \langle value \rangle.
Constraint: \mathbf{pdc} > 0.
```

NE INT 2

```
On entry, \mathbf{pda} = \langle value \rangle and \mathbf{k} = \langle value \rangle.
Constraint: \mathbf{pda} \ge \max(1, \mathbf{k}).
On entry, \mathbf{pdc} = \langle value \rangle and \mathbf{m} = \langle value \rangle.
Constraint: \mathbf{pdc} \ge \max(1, \mathbf{m}).
On entry, \mathbf{pdc} = \langle value \rangle and \mathbf{n} = \langle value \rangle.
Constraint: \mathbf{pdc} \ge \max(1, \mathbf{n}).
```

NE INTERNAL ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG. See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly. See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$||E||_2 = O\epsilon ||C||_2$$

where ϵ is the *machine precision*.

8 Parallelism and Performance

nag_zunmrq (f08cxc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Notefor your implementation for any additional implementation-specific information.

9 Further Comments

The total number of floating-point operations is approximately 8nk(2m-k) if $\mathbf{side} = \text{Nag_LeftSide}$ and 8mk(2n-k) if $\mathbf{side} = \text{Nag_RightSide}$.

The real analogue of this function is nag dormrq (f08ckc).

10 Example

See Section 10 in nag_zgerqf (f08cvc).

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