

# NAG Library Function Document

## nag\_1\_sample\_ks\_test (g08cbc)

### 1 Purpose

nag\_1\_sample\_ks\_test (g08cbc) performs the one sample Kolmogorov–Smirnov test, using one of the distributions provided.

### 2 Specification

```
#include <nag.h>
#include <nagg08.h>

void nag_1_sample_ks_test (Integer n, const double x[],
    Nag_Distributions dist, double par[], Nag_ParaEstimates estima,
    Nag_TestStatistics ntype, double *d, double *z, double *p,
    NagError *fail)
```

### 3 Description

The data consist of a single sample of  $n$  observations denoted by  $x_1, x_2, \dots, x_n$ . Let  $S_n(x_{(i)})$  and  $F_0(x_{(i)})$  represent the sample cumulative distribution function and the theoretical (null) cumulative distribution function respectively at the point  $x_{(i)}$  where  $x_{(i)}$  is the  $i$ th smallest sample observation.

The Kolmogorov–Smirnov test provides a test of the null hypothesis  $H_0$ : the data are a random sample of observations from a theoretical distribution specified by you against one of the following alternative hypotheses:

- (i)  $H_1$ : the data cannot be considered to be a random sample from the specified null distribution.
- (ii)  $H_2$ : the data arise from a distribution which dominates the specified null distribution. In practical terms, this would be demonstrated if the values of the sample cumulative distribution function  $S_n(x)$  tended to exceed the corresponding values of the theoretical cumulative distribution function  $F_0(x)$ .
- (iii)  $H_3$ : the data arise from a distribution which is dominated by the specified null distribution. In practical terms, this would be demonstrated if the values of the theoretical cumulative distribution function  $F_0(x)$  tended to exceed the corresponding values of the sample cumulative distribution function  $S_n(x)$ .

One of the following test statistics is computed depending on the particular alternative null hypothesis specified (see the description of the argument **ntype** in Section 5).

For the alternative hypothesis  $H_1$ .

$D_n$  – the largest absolute deviation between the sample cumulative distribution function and the theoretical cumulative distribution function. Formally  $D_n = \max\{D_n^+, D_n^-\}$ .

For the alternative hypothesis  $H_2$ .

$D_n^+$  – the largest positive deviation between the sample cumulative distribution function and the theoretical cumulative distribution function. Formally  $D_n^+ = \max\{S_n(x_{(i)}) - F_0(x_{(i)}), 0\}$  for both discrete and continuous null distributions.

For the alternative hypothesis  $H_3$ .

$D_n^-$  – the largest positive deviation between the theoretical cumulative distribution function and the sample cumulative distribution function. Formally if the null distribution is discrete then  $D_n^- = \max\{F_0(x_{(i)}) - S_n(x_{(i)}), 0\}$  and if the null distribution is continuous then  $D_n^- = \max\{F_0(x_{(i)}) - S_n(x_{(i-1)}), 0\}$ .

The standardized statistic  $Z = D \times \sqrt{n}$  is also computed where  $D$  may be  $D_n$ ,  $D_n^+$  or  $D_n^-$  depending on the choice of the alternative hypothesis. This is the standardized value of  $D$  with no correction for continuity applied and the distribution of  $Z$  converges asymptotically to a limiting distribution, first derived by Kolmogorov (1933), and then tabulated by Smirnov (1948). The asymptotic distributions for the one-sided statistics were obtained by Smirnov (1933).

The probability, under the null hypothesis, of obtaining a value of the test statistic as extreme as that observed, is computed. If  $n \leq 100$  an exact method given by Conover (1980), is used. Note that the method used is only exact for continuous theoretical distributions and does not include Conover's modification for discrete distributions. This method computes the one-sided probabilities. The two-sided probabilities are estimated by doubling the one-sided probability. This is a good estimate for small  $p$ , that is  $p \leq 0.10$ , but it becomes very poor for larger  $p$ . If  $n > 100$  then  $p$  is computed using the Kolmogorov–Smirnov limiting distributions, see Feller (1948), Kendall and Stuart (1973), Kolmogorov (1933), Smirnov (1933) and Smirnov (1948).

## 4 References

Conover W J (1980) *Practical Nonparametric Statistics* Wiley

Feller W (1948) On the Kolmogorov–Smirnov limit theorems for empirical distributions *Ann. Math. Statist.* **19** 179–181

Kendall M G and Stuart A (1973) *The Advanced Theory of Statistics (Volume 2)* (3rd Edition) Griffin

Kolmogorov A N (1933) Sulla determinazione empirica di una legge di distribuzione *Giornale dell'Istituto Italiano degli Attuari* **4** 83–91

Siegel S (1956) *Non-parametric Statistics for the Behavioral Sciences* McGraw–Hill

Smirnov N (1933) Estimate of deviation between empirical distribution functions in two independent samples *Bull. Moscow Univ.* **2(2)** 3–16

Smirnov N (1948) Table for estimating the goodness of fit of empirical distributions *Ann. Math. Statist.* **19** 279–281

## 5 Arguments

- 1: **n** – Integer *Input*  
*On entry:*  $n$ , the number of observations in the sample.  
*Constraint:*  $n \geq 3$ .
- 2: **x[n]** – const double *Input*  
*On entry:* the sample observations  $x_1, x_2, \dots, x_n$ .  
*Constraint:* the sample observations supplied must be consistent, in the usual manner, with the null distribution chosen, as specified by the arguments **dist** and **par**. For further details see Section 9.
- 3: **dist** – Nag\_Distributions *Input*  
*On entry:* the theoretical (null) distribution from which it is suspected the data may arise.  
**dist** = Nag\_Uniform  
The uniform distribution over  $(a, b)$ .  
**dist** = Nag\_Normal  
The Normal distribution with mean  $\mu$  and variance  $\sigma^2$ .  
**dist** = Nag\_Gamma  
The gamma distribution with shape parameter  $\alpha$  and scale parameter  $\beta$ , where the mean =  $\alpha\beta$ .

**dist** = Nag\_Beta

The beta distribution with shape parameters  $\alpha$  and  $\beta$ , where the mean =  $\alpha/(\alpha + \beta)$ .

**dist** = Nag\_Binomial

The binomial distribution with the number of trials,  $m$ , and the probability of a success,  $p$ .

**dist** = Nag\_Exponential

The exponential distribution with parameter  $\lambda$ , where the mean =  $1/\lambda$ .

**dist** = Nag\_Poisson

The Poisson distribution with parameter  $\mu$ , where the mean =  $\mu$ .

**dist** = Nag\_NegBinomial

The negative binomial distribution with the number of trials,  $m$ , and the probability of success,  $p$ .

**dist** = Nag\_GenPareto

The generalized Pareto distribution with shape parameter  $\xi$  and scale  $\beta$ .

*Constraint:* **dist** = Nag\_Uniform, Nag\_Normal, Nag\_Gamma, Nag\_Beta, Nag\_Binomial, Nag\_Exponential, Nag\_Poisson, Nag\_NegBinomial or Nag\_GenPareto.

4: **par[2]** – double

*Input/Output*

*On entry:* if **estima** = Nag\_ParaSupplied, **par** must contain the known values of the parameter(s) of the null distribution as follows.

If a uniform distribution is used, then **par[0]** and **par[1]** must contain the boundaries  $a$  and  $b$  respectively.

If a Normal distribution is used, then **par[0]** and **par[1]** must contain the mean,  $\mu$ , and the variance,  $\sigma^2$ , respectively.

If a gamma distribution is used, then **par[0]** and **par[1]** must contain the parameters  $\alpha$  and  $\beta$  respectively.

If a beta distribution is used, then **par[0]** and **par[1]** must contain the parameters  $\alpha$  and  $\beta$  respectively.

If a binomial distribution is used, then **par[0]** and **par[1]** must contain the parameters  $m$  and  $p$  respectively.

If an exponential distribution is used, then **par[0]** must contain the parameter  $\lambda$ .

If a Poisson distribution is used, then **par[0]** must contain the parameter  $\mu$ .

If a negative binomial distribution is used, **par[0]** and **par[1]** must contain the parameters  $m$  and  $p$  respectively.

If a generalized Pareto distribution is used, **par[0]** and **par[1]** must contain the parameters  $\xi$  and  $\beta$  respectively.

If **estima** = Nag\_ParaEstimated, **par** need not be set except when the null distribution requested is either the binomial or the negative binomial distribution in which case **par[0]** must contain the parameter  $m$ .

*On exit:* if **estima** = Nag\_ParaSupplied, **par** is unchanged; if **estima** = Nag\_ParaEstimated, and **dist** = Nag\_Binomial or **dist** = Nag\_NegBinomial then **par[1]** is estimated from the data; otherwise **par[0]** and **par[1]** are estimated from the data.

*Constraints:*

if **dist** = Nag\_Uniform, **par[0]** < **par[1]**;

if **dist** = Nag\_Normal, **par[1]** > 0.0;

if **dist** = Nag\_Gamma, **par[0]** > 0.0 and **par[1]** > 0.0;

if **dist** = Nag\_Beta, **par[0]** > 0.0 and **par[1]** > 0.0 and **par[0]** ≤ 10<sup>6</sup> and **par[1]** ≤ 10<sup>6</sup>;

if **dist** = Nag\_Binomial,  $\mathbf{par}[0] \geq 1.0$  and  $0.0 < \mathbf{par}[1] < 1.0$  and  $\mathbf{par}[0] \times \mathbf{par}[1] \times (1.0 - \mathbf{par}[1]) \leq 10^6$  and  $\mathbf{par}[0] < 1/\text{eps}$ , where  $\text{eps} = \textit{machine precision}$ , see nag\_machine\_precision (X02AJC);  
 if **dist** = Nag\_Exponential,  $\mathbf{par}[0] > 0.0$ ;  
 if **dist** = Nag\_Poisson,  $\mathbf{par}[0] > 0.0$  and  $\mathbf{par}[0] \leq 10^6$ ;  
 if **dist** = Nag\_NegBinomial,  $\mathbf{par}[0] \geq 1.0$  and  $0.0 < \mathbf{par}[1] < 1.0$  and  $\mathbf{par}[0] \times (1.0 - \mathbf{par}[1]) / (\mathbf{par}[1] \times \mathbf{par}[1]) \leq 10^6$  and  $\mathbf{par}[0] < 1/\text{eps}$ , where  $\text{eps} = \textit{machine precision}$ , see nag\_machine\_precision (X02AJC);  
 if **dist** = Nag\_GenPareto,  $\mathbf{par}[1] > 0$ .

5: **estima** – Nag\_ParaEstimates *Input*

*On entry:* **estima** must specify whether values of the parameters of the null distribution are known or are to be estimated from the data.

**estima** = Nag\_ParaSupplied

Values of the parameters will be supplied in the array **par** described above.

**estima** = Nag\_ParaEstimated

Parameters are to be estimated from the data except when the null distribution requested is the binomial distribution or the negative binomial distribution in which case the first parameter,  $m$ , must be supplied in **par**[0] and only the second parameter,  $p$ , is estimated from the data.

*Constraint:* **estima** = Nag\_ParaSupplied or Nag\_ParaEstimated.

6: **ntype** – Nag\_TestStatistics *Input*

*On entry:* the test statistic to be calculated, i.e., the choice of alternative hypothesis.

**ntype** = Nag\_TestStatisticsDAbs

Computes  $D_n$ , to test  $H_0$  against  $H_1$ ,

**ntype** = Nag\_TestStatisticsDPos

Computes  $D_n^+$ , to test  $H_0$  against  $H_2$ ,

**ntype** = Nag\_TestStatisticsDNeg

Computes  $D_n^-$ , to test  $H_0$  against  $H_3$ .

*Constraint:* **ntype** = Nag\_TestStatisticsDAbs, Nag\_TestStatisticsDPos or Nag\_TestStatisticsDNeg.

7: **d** – double \* *Output*

*On exit:* the Kolmogorov–Smirnov test statistic ( $D_n$ ,  $D_n^+$  or  $D_n^-$  according to the value of **ntype**).

8: **z** – double \* *Output*

*On exit:* a standardized value,  $Z$ , of the test statistic,  $D$ , without any correction for continuity.

9: **p** – double \* *Output*

*On exit:* the probability,  $p$ , associated with the observed value of  $D$  where  $D$  may be  $D_n$ ,  $D_n^+$  or  $D_n^-$  depending on the value of **ntype** (see Section 3).

10: **fail** – NagError \* *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

See Section 3.2.1.2 in How to Use the NAG Library and its Documentation for further information.

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_G08CB\_DATA

On entry, **dist** = Nag\_Beta and at least one observation is illegal.

Constraint:  $0 \leq x[i-1] \leq 1$ , for  $i = 1, 2, \dots, n$ .

On entry, **dist** = Nag\_Binomial and all observations are zero or  $m$ .

Constraint: at least one  $0.0 < x[i-1] < \mathbf{par}[0]$ , for  $i = 1, 2, \dots, n$ .

On entry, **dist** = Nag\_Binomial and at least one observation is illegal.

Constraint:  $0 \leq x[i-1] \leq \mathbf{par}[0]$ , for  $i = 1, 2, \dots, n$ .

On entry, **dist** = Nag\_Exponential or Nag\_Poisson and all observations are zero.

Constraint: at least one  $x[i-1] > 0$ , for  $i = 1, 2, \dots, n$ .

On entry, **dist** = Nag\_Gamma, Nag\_Exponential, Nag\_Poisson, Nag\_NegBinomial or Nag\_GenPareto and at least one observation is negative.

Constraint:  $x[i-1] \geq 0$ , for  $i = 1, 2, \dots, n$ .

On entry, **dist** = Nag\_Uniform and at least one observation is illegal.

Constraint:  $\mathbf{par}[0] \leq x[i-1] \leq \mathbf{par}[1]$ , for  $i = 1, 2, \dots, n$ .

### NE\_G08CB\_PARAM

On entry, **dist** = Nag\_Binomial and  $m = \mathbf{par}[0] = \langle value \rangle$ .

Note that  $m$  must always be supplied.

Constraint: for the binomial distribution,  $1 \leq \mathbf{par}[0] < 1/\text{eps}$ , where  $\text{eps} = \textit{machine precision}$ , see nag\_machine\_precision (X02AJC).

On entry, **dist** = Nag\_GenPareto and **estima** = Nag\_ParaEstimated.

The parameter estimates are invalid; the data may not be from the generalized Pareto distribution.

On entry, **dist** = Nag\_NegBinomial and  $m = \mathbf{par}[0] = \langle value \rangle$ .

Note that  $m$  must always be supplied.

Constraint: for the negative binomial distribution,  $1 \leq \mathbf{par}[0] < 1/\text{eps}$ , where  $\text{eps} = \textit{machine precision}$ , see nag\_machine\_precision (X02AJC).

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ ;  $\mathbf{par}[1] = \langle value \rangle$ .

Constraint: for the beta distribution,  $0 < \mathbf{par}[0]$  and  $\mathbf{par}[1] \leq 1000000$ .

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ ;  $\mathbf{par}[1] = \langle value \rangle$ .

Constraint: for the gamma distribution,  $\mathbf{par}[0]$  and  $\mathbf{par}[1] > 0$ .

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ ;  $\mathbf{par}[1] = \langle value \rangle$ .

Constraint: for the generalized Pareto distribution with  $\mathbf{par}[0] < 0$ ,  $0 \leq x[i-1] \leq -\mathbf{par}[1]/\mathbf{par}[0]$ , for  $i = 1, 2, \dots, n$ .

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ ;  $\mathbf{par}[1] = \langle value \rangle$ .

Constraint: for the uniform distribution,  $\mathbf{par}[0] < \mathbf{par}[1]$ .

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ .

Constraint: for the exponential distribution,  $\mathbf{par}[0] > 0$ .

On entry, **estima** = Nag\_ParaSupplied and  $\mathbf{par}[0] = \langle value \rangle$ .

Constraint: for the Poisson distribution,  $0 < \mathbf{par}[0] < 1000000$ .

On entry, **estima** = Nag\_ParaSupplied and **par**[1] =  $\langle value \rangle$ .

Constraint: for the binomial distribution,  $0 < \mathbf{par}[1] < 1$ .

On entry, **estima** = Nag\_ParaSupplied and **par**[1] =  $\langle value \rangle$ .

Constraint: for the generalized Pareto distribution, **par**[1] > 0.

On entry, **estima** = Nag\_ParaSupplied and **par**[1] =  $\langle value \rangle$ .

Constraint: for the negative binomial distribution,  $0 < \mathbf{par}[1] < 1$ .

On entry, **estima** = Nag\_ParaSupplied and **par**[1] =  $\langle value \rangle$ .

Constraint: for the Normal distribution, **par**[1] > 0.

### NE\_G08CB\_SAMPLE

On entry, **dist** = Nag\_Uniform, Nag\_Normal, Nag\_Gamma, Nag\_Beta or Nag\_GenPareto, **estima** = Nag\_ParaEstimated and the whole sample is constant. Thus the variance is zero.

### NE\_G08CB\_VARIANCE

On entry, **dist** = Nag\_Binomial, **par**[0] =  $\langle value \rangle$ , **par**[1] =  $\langle value \rangle$ .

The variance **par**[0] × **par**[1] × (1 - **par**[1]) exceeds 1000000.

On entry, **dist** = Nag\_NegBinomial, **par**[0] =  $\langle value \rangle$ , **par**[1] =  $\langle value \rangle$ .

The variance **par**[0] × (1 - **par**[1]) / (**par**[1] × **par**[1]) exceeds 1000000.

### NE\_INT\_ARG\_LT

On entry, **n** =  $\langle value \rangle$ .

Constraint: **n** ≥ 3.

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 3.6.6 in How to Use the NAG Library and its Documentation for further information.

### NE\_NO\_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 3.6.5 in How to Use the NAG Library and its Documentation for further information.

## 7 Accuracy

The approximation for  $p$ , given when  $n > 100$ , has a relative error of at most 2.5% for most cases. The two-sided probability is approximated by doubling the one-sided probability. This is only good for small  $p$ , i.e.,  $p < 0.10$  but very poor for large  $p$ . The error is always on the conservative side, that is the tail probability,  $p$ , is over estimated.

## 8 Parallelism and Performance

nag\_1\_sample\_ks\_test (g08cbc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

## 9 Further Comments

The time taken by `nag_1_sample_ks_test` (g08cbc) increases with  $n$  until  $n > 100$  at which point it drops and then increases slowly with  $n$ . The time may also depend on the choice of null distribution and on whether or not the parameters are to be estimated.

The data supplied in the argument  $\mathbf{x}$  must be consistent with the chosen null distribution as follows:

- when **dist** = Nag-Uniform, then  $\mathbf{par}[0] \leq x_i \leq \mathbf{par}[1]$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-Normal, then there are no constraints on the  $x_i$ 's;
- when **dist** = Nag-Gamma, then  $x_i \geq 0.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-Beta, then  $0.0 \leq x_i \leq 1.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-Binomial, then  $0.0 \leq x_i \leq \mathbf{par}[0]$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-Exponential, then  $x_i \geq 0.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-Poisson, then  $x_i \geq 0.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-NegBinomial, then  $x_i \geq 0.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-GenPareto and  $\mathbf{par}[0] \geq 0.0$ , then  $x_i \geq 0.0$ , for  $i = 1, 2, \dots, n$ ;
- when **dist** = Nag-GenPareto and  $\mathbf{par}[0] < 0.0$ , then  $0.0 \leq x_i \leq -\mathbf{par}[1]/\mathbf{par}[0]$ , for  $i = 1, 2, \dots, n$ .

## 10 Example

The following example program reads in a set of data consisting of 30 observations. The Kolmogorov–Smirnov test is then applied twice, firstly to test whether the sample is taken from a uniform distribution,  $U(0, 2)$ , and secondly to test whether the sample is taken from a Normal distribution where the mean and variance are estimated from the data. In both cases we are testing against  $H_1$ ; that is, we are doing a two tailed test. The values of  $\mathbf{d}$ ,  $\mathbf{z}$  and  $\mathbf{p}$  are printed for each case.

### 10.1 Program Text

```

/* nag_1_sample_ks_test (g08cbc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg08.h>

int main(void)
{
    Integer exit_status = 0;
    Integer i, n, np;
    double d, p, *par = 0, *x = 0, z;
    char nag_enum_arg[40];
    Nag_TestStatistics ntype;
    NagError fail;

    INIT_FAIL(fail);

    printf("nag_1_sample_ks_test (g08cbc) Example Program Results\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n]");

```

```

#else
    scanf("%*[^\\n]");
#endif

#ifdef _WIN32
    scanf_s("%" NAG_IFMT "", &n);
#else
    scanf("%" NAG_IFMT "", &n);
#endif
    x = NAG_ALLOC(n, double);

    printf("\\n");
    for (i = 1; i <= n; ++i)
#ifdef _WIN32
        scanf_s("%lf", &x[i - 1]);
#else
        scanf("%lf", &x[i - 1]);
#endif
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "", &np);
#else
    scanf("%" NAG_IFMT "", &np);
#endif
    if (!(par = NAG_ALLOC(np, double)))
    {
        printf("Allocation failure\\n");
        exit_status = -1;
        goto END;
    }

    for (i = 1; i <= np; ++i)
#ifdef _WIN32
        scanf_s("%lf", &par[i - 1]);
#else
        scanf("%lf", &par[i - 1]);
#endif
#ifdef _WIN32
    scanf_s("%39s", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac).
     * Converts NAG enum member name to value
     */
    ntype = (Nag_TestStatistics) nag_enum_name_to_value(nag_enum_arg);

    /* nag_1_sample_ks_test (g08cbc).
     * Performs the one-sample Kolmogorov-Smirnov test for
     * standard distributions
     */
    nag_1_sample_ks_test(n, x, Nag_Uniform, par, Nag_ParaSupplied, ntype, &d,
                        &z, &p, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_1_sample_ks_test (g08cbc).\\n%s\\n", fail.message);
        exit_status = 1;
        goto END;
    }
    printf("Test against uniform distribution on (0,2)\\n");
    printf("\\n");
    printf("Test statistic D = %8.4f\\n", d);
    printf("Z statistic      = %8.4f\\n", z);
    printf("Tail probability = %8.4f\\n", p);
    printf("\\n");
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "", &np);
#else
    scanf("%" NAG_IFMT "", &np);
#endif
    for (i = 1; i <= np; ++i)
#ifdef _WIN32
        scanf_s("%lf", &par[i - 1]);

```



```

#else
    scanf("%lf", &par[i - 1]);
#endif
#ifdef _WIN32
    scanf_s("%39s", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s", nag_enum_arg);
#endif
    ntype = (Nag_TestStatistics) nag_enum_name_to_value(nag_enum_arg);

    /* nag_1_sample_ks_test (g08cbc), see above. */
    nag_1_sample_ks_test(n, x, Nag_Normal, par, Nag_ParaEstimated, ntype, &d,
        &z, &p, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_1_sample_ks_test (g08cbc).\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    printf("Test against Normal distribution with parameters estimated"
        " from the data\n\n");
    printf("Mean = %6.4f and variance = %6.4f\n", par[0], par[1]);
    printf("Test statistic D = %8.4f\n", d);
    printf("Z statistic      = %8.4f\n", z);
    printf("Tail probability = %8.4f\n", p);

END:
    NAG_FREE(x);
    NAG_FREE(par);

    return exit_status;
}

```

## 10.2 Program Data

```

nag_1_sample_ks_test (g08cbc) Example Program Data
30
0.01 0.30 0.20 0.90 1.20 0.09 1.30 0.18 0.90 0.48
1.98 0.03 0.50 0.07 0.70 0.60 0.95 1.00 0.31 1.45
1.04 1.25 0.15 0.75 0.85 0.22 1.56 0.81 0.57 0.55
2 0.0 2.0 Nag_TestStatisticsDabs
2 0.0 1.0 Nag_TestStatisticsDabs

```

## 10.3 Program Results

```

nag_1_sample_ks_test (g08cbc) Example Program Results

```

```

Test against uniform distribution on (0,2)

```

```

Test statistic D = 0.2800
Z statistic      = 1.5336
Tail probability = 0.0143

```

```

Test against Normal distribution with parameters estimated from the data

```

```

Mean = 0.6967 and variance = 0.2564
Test statistic D = 0.1108
Z statistic      = 0.6068
Tail probability = 0.8925

```

---